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# COMM 204 (TIM HUH) FINAL EXAM REVIEW SESSION

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# FORECASTING

Sales of Honda Civics have grown steadily at auto dealerships in Vancouver during the past 5 years. The sales manager had predicted before the new model was introduced that first year sales would be 410 cars. Using exponential smoothing with a weight of  $\alpha=0.30$ , develop forecasts for years 2 through 6.

| Year | Sales | Forecast                         |
|------|-------|----------------------------------|
| 1    | 450   | 410                              |
| 2    | 495   | $410+0.3(450-410) = 422$         |
| 3    | 518   | $422+0.3(495-422) = 443.9$       |
| 4    | 563   | $443.9+0.3(518-443.9) = 466.1$   |
| 5    | 584   | $466.1+0.3(563-466.1) = 495.2$   |
| 6    | 600   | $495.2 + 0.3(584-495.2) = 521.8$ |

Redo the previous question but forecast using the Naïve approach:

| Year | Sales | Forecast |
|------|-------|----------|
| 1    | 450   | 410      |
| 2    | 495   | 450      |
| 3    | 518   | 495      |
| 4    | 563   | 518      |
| 5    | 584   | 563      |
| 6    | 600   | 584      |



A large Portland manufacturer wants to forecast demand for a piece of pollution-control equipment. A review of past sales, as shown below, indicates that an increasing trend is present:

| Month | Actual Demand | Month | Actual Demand |
|-------|---------------|-------|---------------|
| 1     | 12            | 6     | 21            |
| 2     | 17            | 7     | 31            |
| 3     | 20            | 8     | 28            |
| 4     | 19            | 9     | 36            |
| 5     | 24            | 10    | ?             |

Smoothing constants are assigned the values of  $\alpha=0.2$  and  $\beta=0.4$ . The firm assumes the initial forecast average for month 1 ( $F_1$ ) was 11 units and the trend over the period ( $T_1$ ) was 2 units.

a) Forecast average for month 2:

$$F_2 = \alpha A_1 + (1-\alpha)(F_1 + T_1)$$

$$F_2 = (0.2)(12) + (1-0.2)(11+2) = 2.4 + 10.4 = 12.8 \text{ units}$$

b) Compute the trend in period 2:

$$T_2 = \beta(F_2 - F_1) + (1-\beta)T_1$$

$$T_2 = 0.4(12.8-11) + (1-0.4)(2) = 0.71+1.2 = 1.92$$

c) Compute the forecast including trend ( $FIT_t$ )

$$FIT_2 = F_2 + T_2 = 12.8 + 1.92 = 14.72 \text{ units}$$

Compute MAD and MSE from the following data of a regression line projection:

| Period | Forecast Values | Actual Values |
|--------|-----------------|---------------|
| 1      | 410             | 406           |
| 2      | 419             | 423           |
| 3      | 428             | 423           |
| 4      | 435             | 440           |

$$MAD = \frac{\sum |Actual - Forecast|}{n} = \frac{|406-410| + |423-419| + |423-428| + |440-435|}{4} = \frac{18}{4} = 4.5$$

$$MSE = \frac{\sum (Forecast Errors)^2}{n} = \frac{4^2 + 4^2 + 5^2 + 5^2}{4} = 20.5$$

# Inventory Model

Annual demand for a product is 5000 units; holding cost is \$50 per unit per year. Setup cost is \$30 per order; and lead time has a 10 day average. Suppose there are 250 working days per year.

a) What is the EOQ?

$$\begin{aligned}Q_{\text{opt}} &= \sqrt{2SD/H} \\&= \sqrt{2(30)(5000)/(50)} \\&= \sqrt{6000} \\&= 77.46 = 78 \text{ units}\end{aligned}$$

b) What is the avg. inventory?

$$\begin{aligned}&= Q/2 \\&= 78/2 = 39 \text{ units}\end{aligned}$$

c) What is the optimal number of orders to place in a year?

$$\begin{aligned}&= D/Q \\&= 5000/78 \\&= 64.1 = 65\end{aligned}$$

d) What is the optimal number of working days between any two orders?

$$\begin{aligned}&= \text{Number of working days} / \text{Expected number of orders} \\&= 250 \text{ days} / 65 \\&= 3.85 \text{ days}\end{aligned}$$

e) What is the total annual cost?

$$\begin{aligned}TC &= \frac{D}{Q} S + \frac{Q}{2} H \\TC &= \frac{5000}{78} (30) + \frac{78}{2} (50) = \$3873.08\end{aligned}$$

f) What is the ROP?

$$\begin{aligned}ROP &= D * LT \\&= 5000 * 10/250 \\&= 200\end{aligned}$$



Demand during lead time for a product follows a normal distribution with a mean of 36 and a standard deviation of 15. What safety stock should be kept to achieve a 90% service level? What is the ROP?

$$z = 1.28$$

$$SS = 1.28 * 15 = 19.22$$

$$ROP = 36 + 19.22 = 55.22$$

Kristen sells pies for \$10 each. Unsold pies are sold at a 50% discount. The cost for each pie is \$6, and demand follows a normal distribution with a mean of 25 and s.d. of 4.

What is the optimal stocking level?

$$\text{Service level} = 4 / (4+1) = 0.8$$

$$Z\text{-score}(0.8)=0.84$$

$$\text{Optimal stocking level} = 25 + 0.84(4) = 28.36 = 29 \text{ pies}$$

A company sells 20000 tires each year. The setup cost is \$40 per order. The holding cost is \$20% of the purchase price of each tire. The purchase price varies according the quantity below. How many tires should the company order each time?

| Quantity                        | Purchase Price per Tire |
|---------------------------------|-------------------------|
| Less than 500                   | \$20                    |
| 500 or more, but less than 1000 | \$18                    |
| 1000 or more                    | \$17                    |

$$Q_{\text{opt at } \$20} = \sqrt{2SD/H} = \sqrt{\frac{2(40)(20000)}{0.2*20}} = 632.46$$

$$Q_{\text{opt at } \$18} = \sqrt{\frac{2(40)(20000)}{0.2*18}} = 666.67$$

This one is in the quantity range.

$$Q_{\text{opt at } \$17} = \sqrt{\frac{2(40)(20000)}{0.2*17}} = 685.99$$



The daily demand for 52" flat-screen TVs is normally distributed, with an average of 5 and a standard deviation of 2 units. The lead time for receiving a shipment of new TVs is 10 days and is constant. Determine the reorder point and safety stock for a 95% service level

$$ROP = (\text{Average daily demand} \times \text{Lead time in days}) + Z\sigma_{dLT}$$

$$\text{Where } \sigma_{dLT} = \sigma_d \sqrt{\text{Lead time}}$$

So, with  $Z = 1.65$  ← confidence of 95%

$$ROP = (5 \times 10) + 1.65(2)\sqrt{10} = 50 + 10.4 = 60.4 = 61 \text{ TVs}$$

Safety stock is 10.4 or 11 TVs

The KEY Electronics store purchases calculators from the manufacturer at \$4 per unit. The setup cost is \$75 per order, and holding cost is based on a 20% annual interest rate. Finally, the shortage cost per unit of stockout is \$25. Expected annual demand is 624 units, demand during the delivery lead-time from the manufacturer to the KEY Electronics store is normally distributed with a mean of 36 and variance of 48.

a) Find the EOQ for the KEY Electronics assuming that there is no shortage cost.

$$EOQ = \sqrt{(2)(75)(624)/(0.2)(4)}$$

b) Find the optimal (Q,r) policy, where the safety stock is chosen to minimize the expected sum of holding cost and shortage cost. (Hint: use the newsvendor model for each order cycle to determine Z).

The unit overage cost is the unit holding cost during one cycle, which is  $C_o = H \times \frac{Q}{D} = 20\% \times 4 \times \frac{342}{624} = \$0.438$ , (Q/D is the cycle time); whereas the unit underage cost is the unit shortage cost in one cycle, which is \$25. So the critical ratio  $\frac{C_u}{C_o + C_u} = 25/(25 + 0.438) = 0.9825$ . The z-score of 98.25% is 2.1106. So the safety stock is  $SS = Z\sigma_{LT} = 2.1106 \times \sqrt{48} = 14.6$ .

Thus,  $Q = 342$ ,  $r = SS + \mu_{LT} = 50.6$